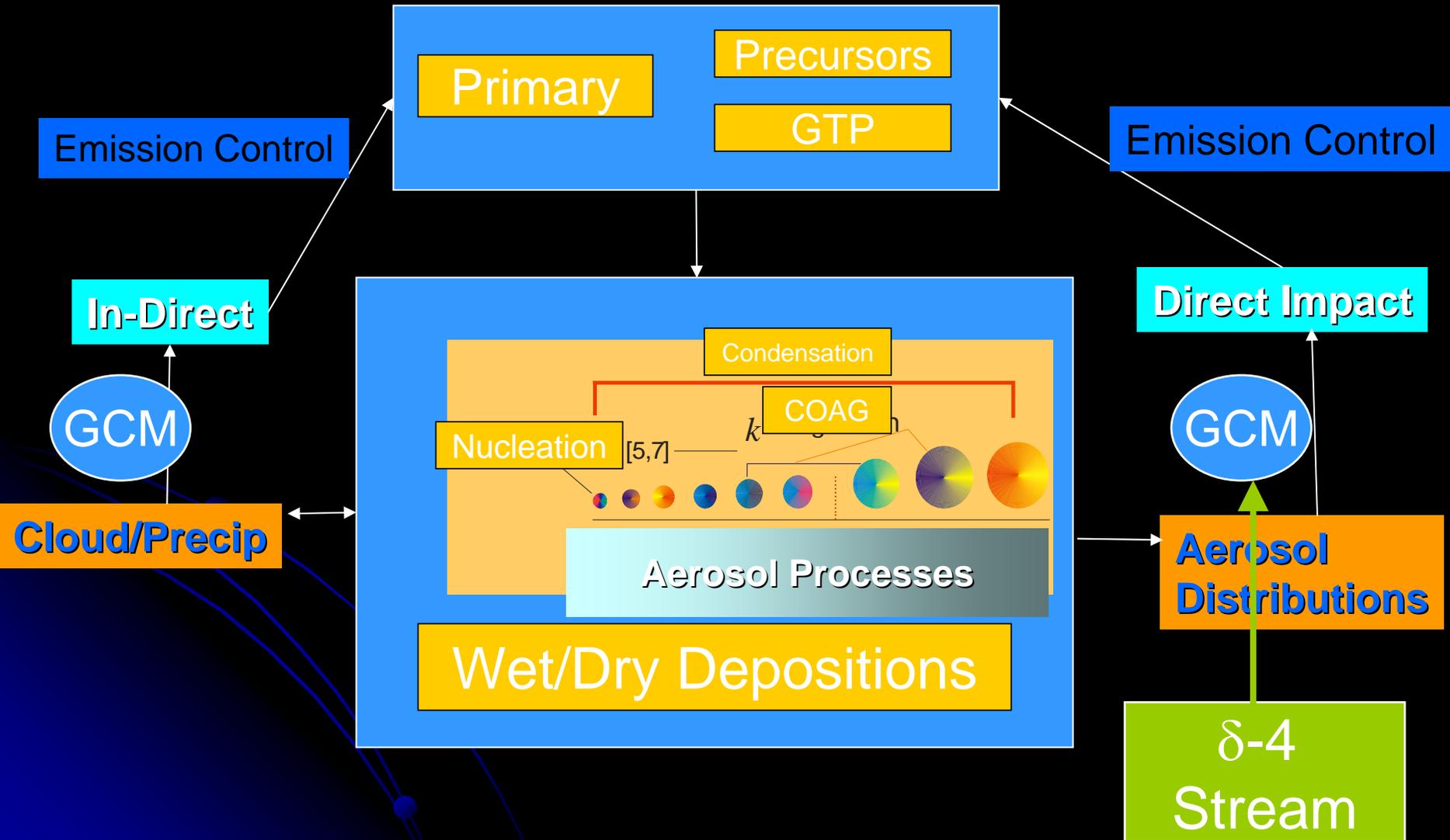


# Aerosol Climate Impact Assessment



# Implementing the Delta-Four-Stream Approximation for Solar Radiation Computations in the CCC AGCM III

By

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# Outline

1. Introduction
2. Solar Flux Simulations
3. Computational Time
4. Conclusions and Recommendations

# Introduction

- Solar-radiation computation: fundamental in climate modeling
- Radiative transfer eq. for a plane-parallel homog. atmos.

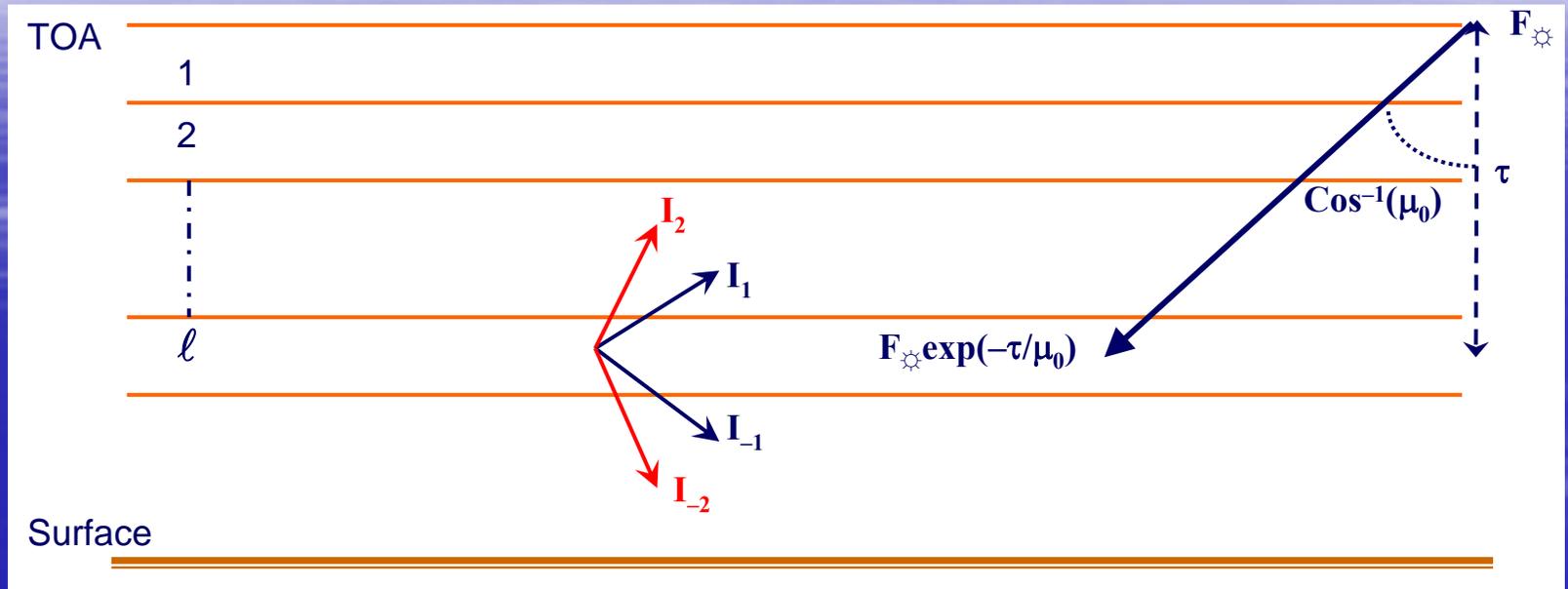
$$\mu \frac{dI(\tau, \mu)}{d\tau} = I(\tau, \mu) - \frac{\tilde{\omega}}{2} \int_{-1}^1 I(\tau, \mu') \cdot P(\mu, \mu') d\mu' - \frac{\tilde{\omega}}{4\pi} F_{\odot} P(\mu, -\mu_0) \cdot e^{-\tau/\mu_0}$$

- Gauss-exp. for intensity & Legendre-exp. for phase func.

$$\mu_i \frac{dI(\tau, \mu_i)}{d\tau} = I(\tau, \mu_i) - \frac{\tilde{\omega}}{2} \sum_{l=0}^N \tilde{\omega}_l P_l(\mu_i) \sum_{j=-n}^n a_j P_l(\mu_j) I(\tau, \mu_j) - \frac{\tilde{\omega}}{4\pi} F_{\odot} \left[ \sum_{l=0}^N (-1)^l \tilde{\omega}_l P_l(\mu_i) P_l(\mu_0) \right] \cdot e^{-\tau/\mu_0}$$

- GCM-coupled models: computational constraints
- Resort to simplest two-stream approximations

# Introduction



- CCC GCM III: SW layer reflectance and transmittance  
clear-sky: 2-stream (TS), whole-sky:  $\delta$ -Eddington (DE)
- $\delta$ -four-stream (DFS): matrix formulation by Liou *et al.* (1988)  
compromise between accuracy & efficiency

# Introduction

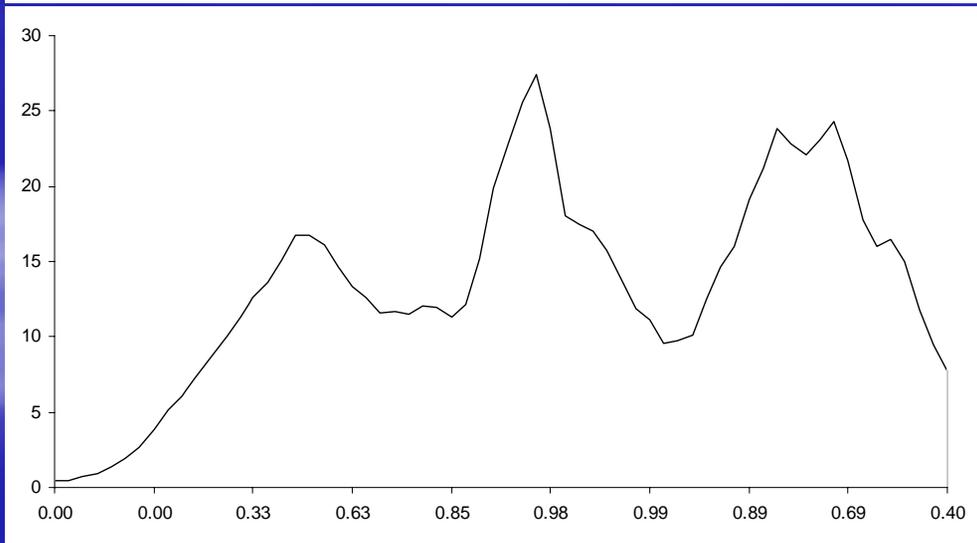
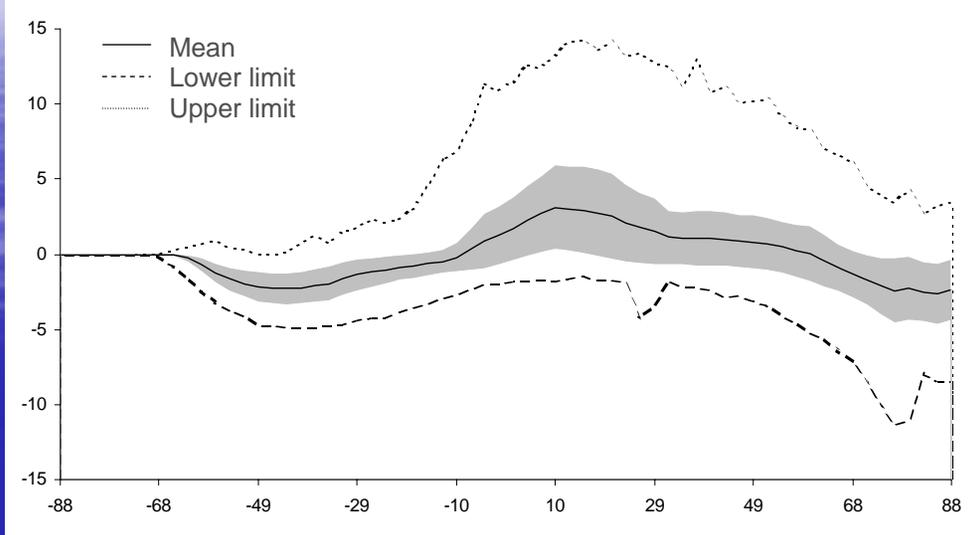
- Code input: Layer cloud fraction, optical depth, single-scattering albedo (SSA), asymmetry factor; underlying albedo, cosine of solar zenith angle (CSZA)
- Code output:
  - DE-equivalent: Layer reflectance & transmittance, with & without reflection from underlying surface  
Follow from original DFS formulation by solving BVP
  - TS-equivalent: Layer reflectance & transmittance, with multiple/single reflection from underlying surface  
Some manipulation to derive layer reflectance with single reflection

# Introduction

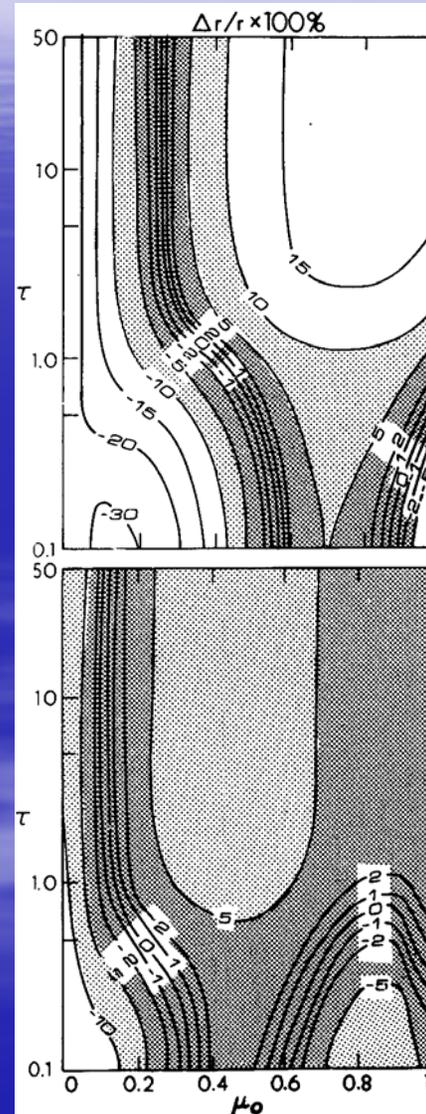
- GCM run for 2 years (six months for spin-up)
- Parallel calls to shortwave radiation routine, with original & DFS-modified codes, at every model-hour
- Include optical properties of aerosols simulated by CAM
- Examine changes in modeled SW flux at TOA and surface

# Solar Flux Simulations

July-zonal mean of diff. in surf. whole-sky, SW flux ( $Wm^{-2}$ )



July-zonal mean of column-integrated cloud optical depth for 1<sup>st</sup> solar band (0.25 – 0.69  $\mu m$ ) vs. maximum CSZA



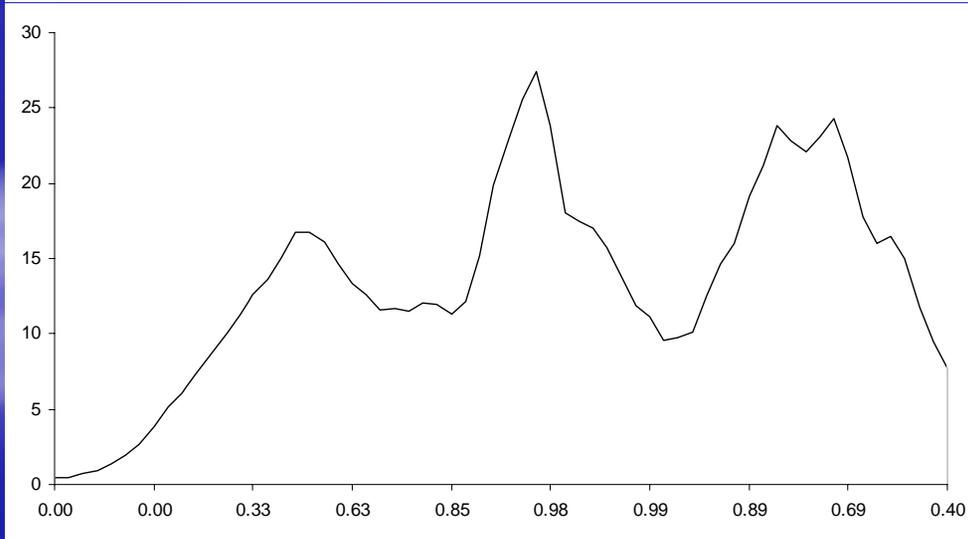
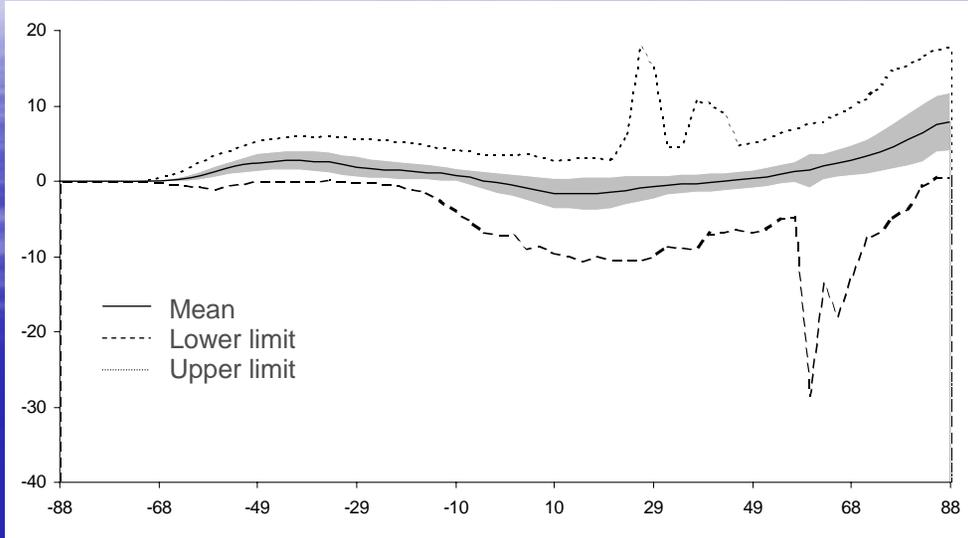
DTS

Relative accuracy (%) of reflectance from DTS & DFS with respect to adding method, at SSA of 0.8 (Liou *et al.* 1988).

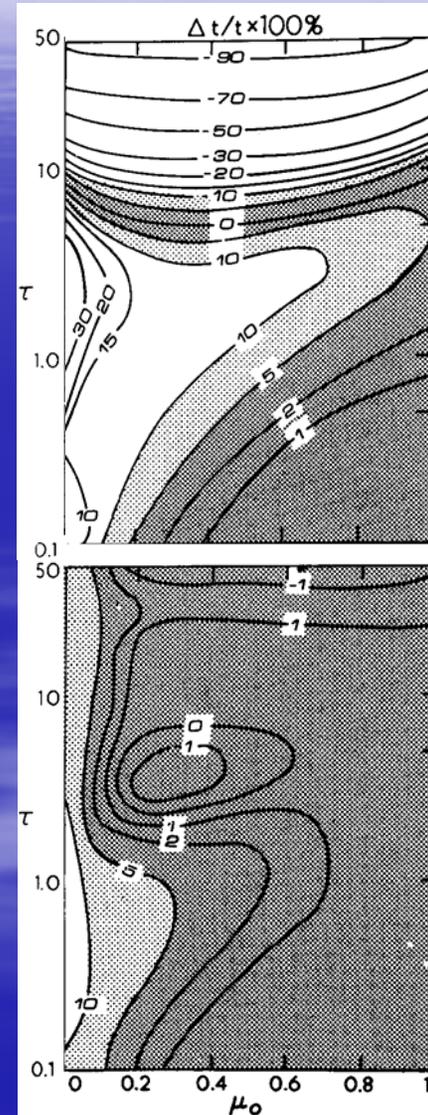
DFS

# Solar Flux Simulations

July-zonal mean of diff. in surf. whole-sky, SW flux ( $\text{Wm}^{-2}$ )



July-zonal mean of column-integrated cloud optical depth for 1<sup>st</sup> solar band ( $0.25 - 0.69 \mu\text{m}$ ) vs. maximum CSZA



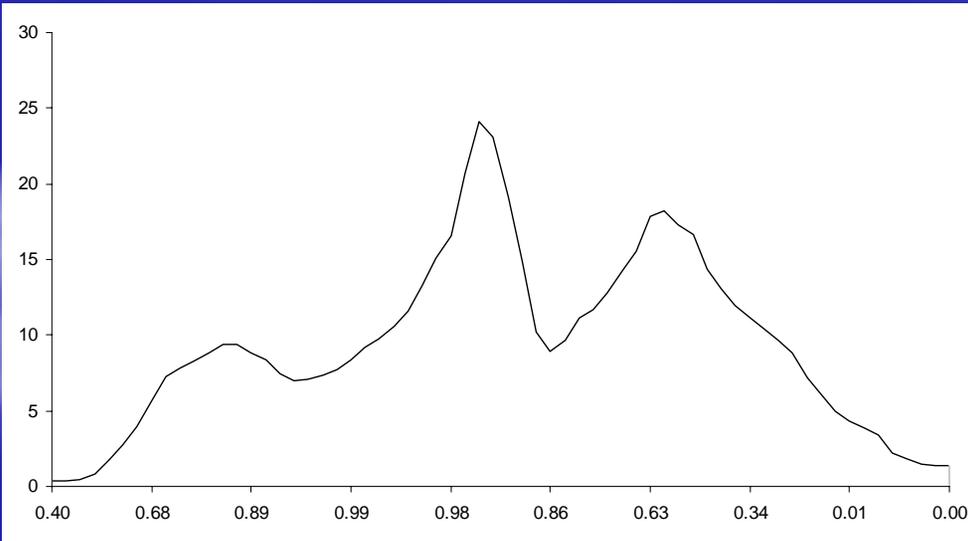
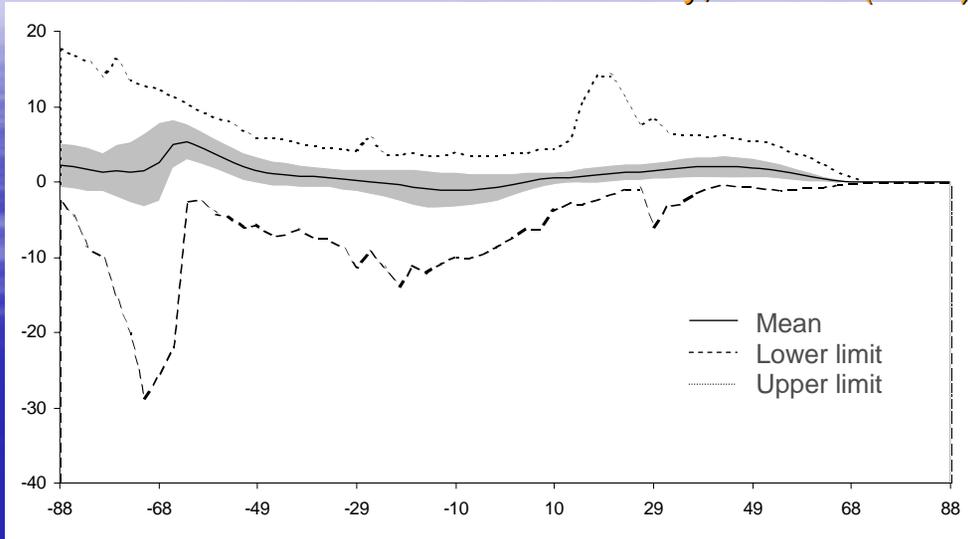
DTS

Relat. accuracy (%) of transmittance from DTS & DFS with respect to adding method, at SSA of 0.8 (Liou *et al.* 1988).

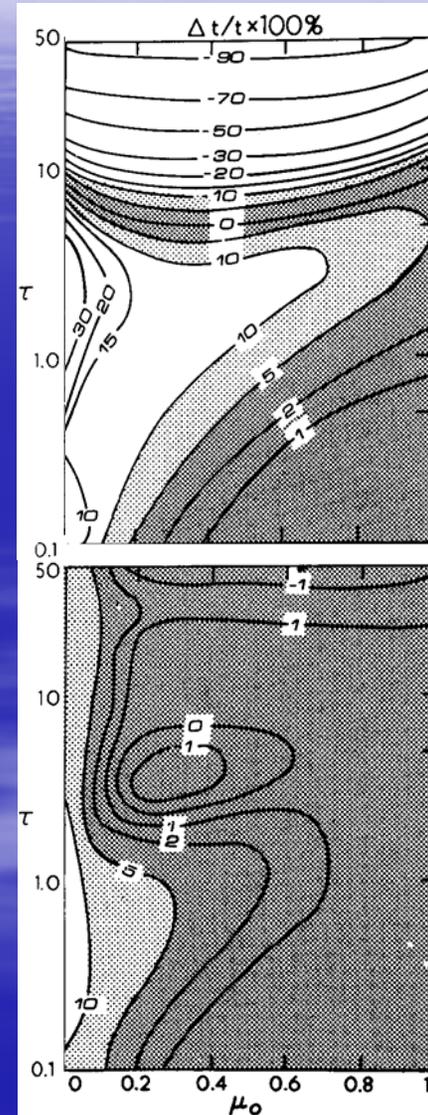
DFS

# Solar Flux Simulations

Jan-zonal mean of diff. in surf. whole-sky, SW flux ( $Wm^{-2}$ )



Jan-zonal mean of column-integrated cloud optical depth for 1<sup>st</sup> solar band (0.25 – 0.69  $\mu m$ ) vs. maximum CSZA



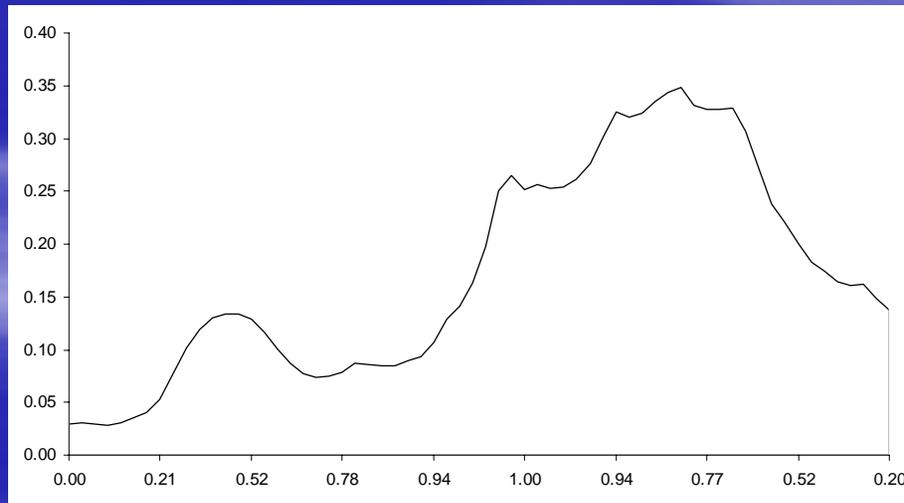
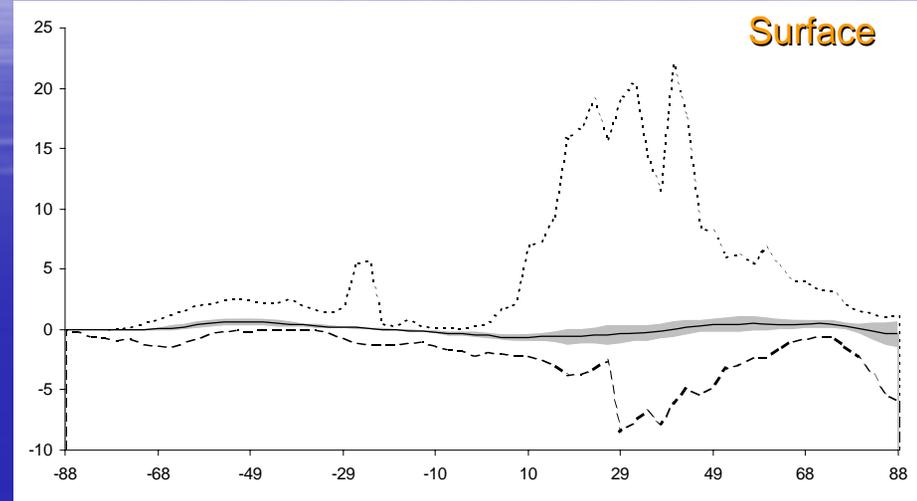
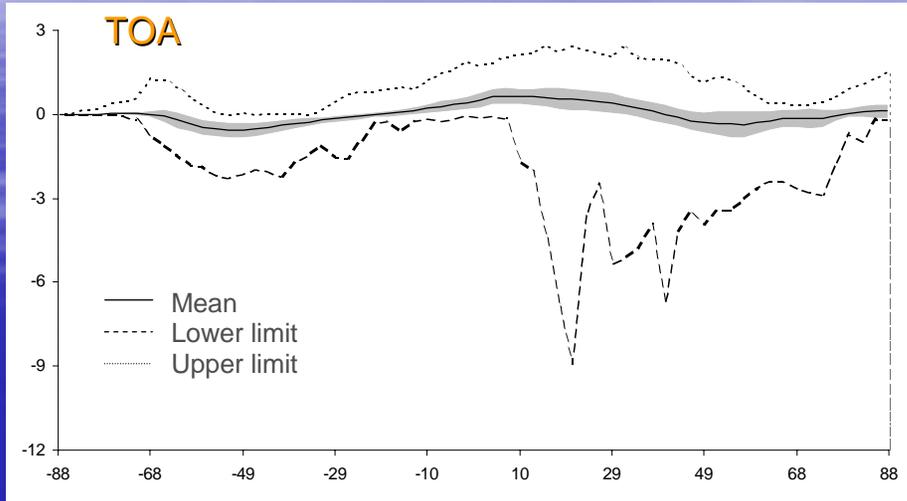
DTS

Relat. accuracy (%)  
of transmittance  
from DTS & DFS  
with respect to  
adding method, at  
SSA of 0.8  
(Liou *et al.* 1988).

DFS

# Solar Flux Simulations

April-zonal mean of diff. in clear-sky, SW flux ( $Wm^{-2}$ )



April-zonal mean of column-integrated aerosol optical depth at  $0.55 \mu m$  vs. maximum CSZA

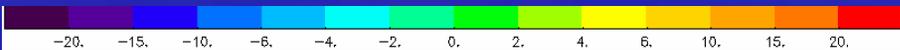
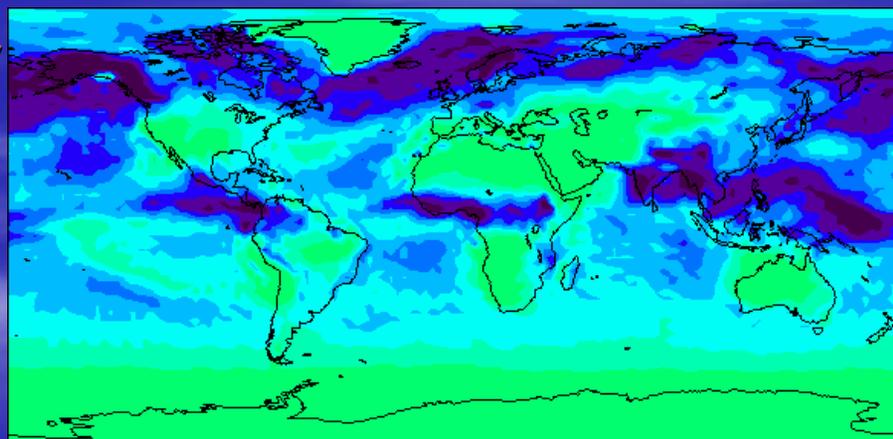
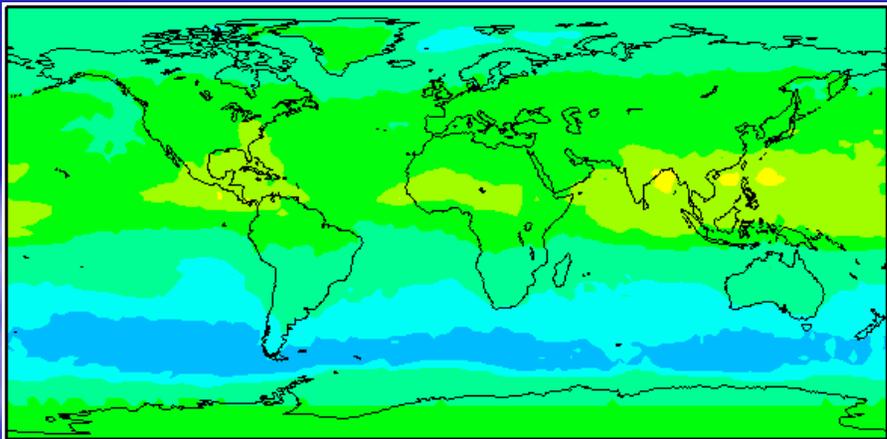
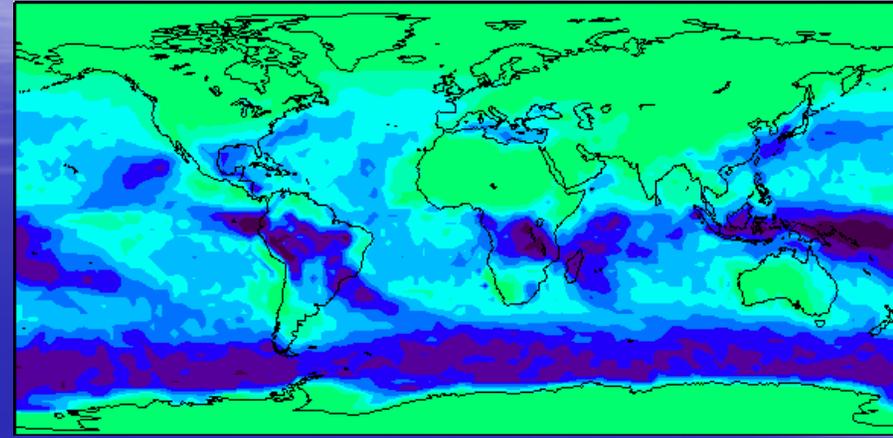
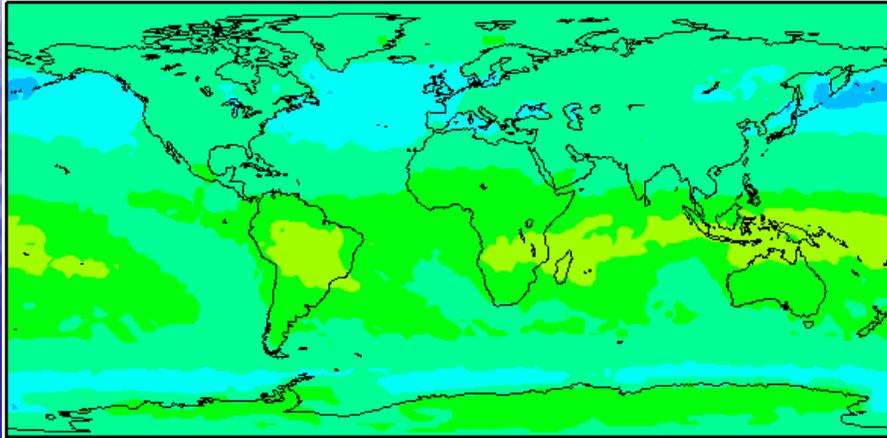
# Solar Flux Simulations

Mean percentage diff. in TOA whole-sky SW flux

Mean TOA SW cloud radiative forcing ( $Wm^{-2}$ )

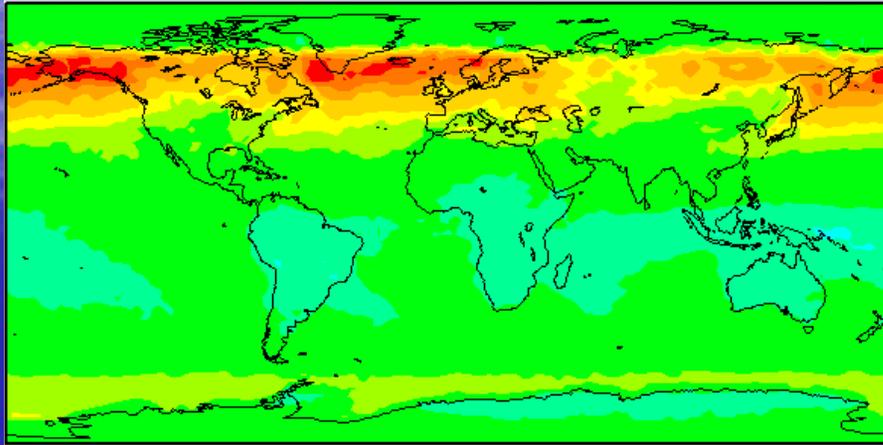
Jan

July

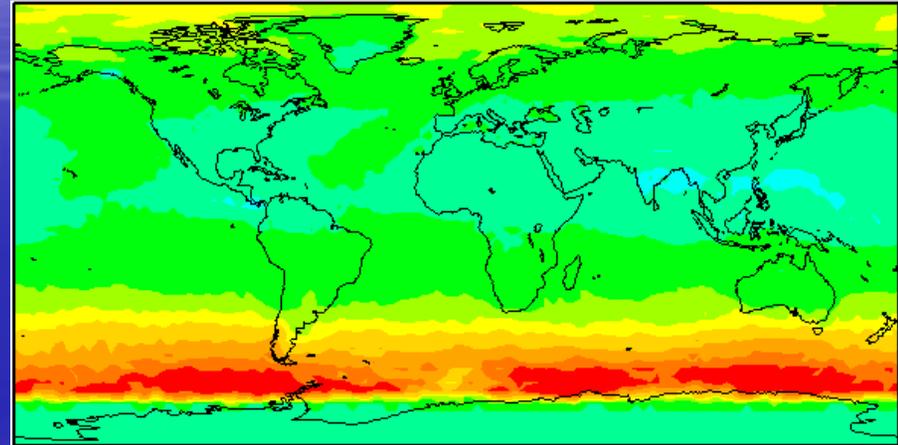


# Solar Flux Simulations

Mean percentage diff. in surface whole-sky SW flux



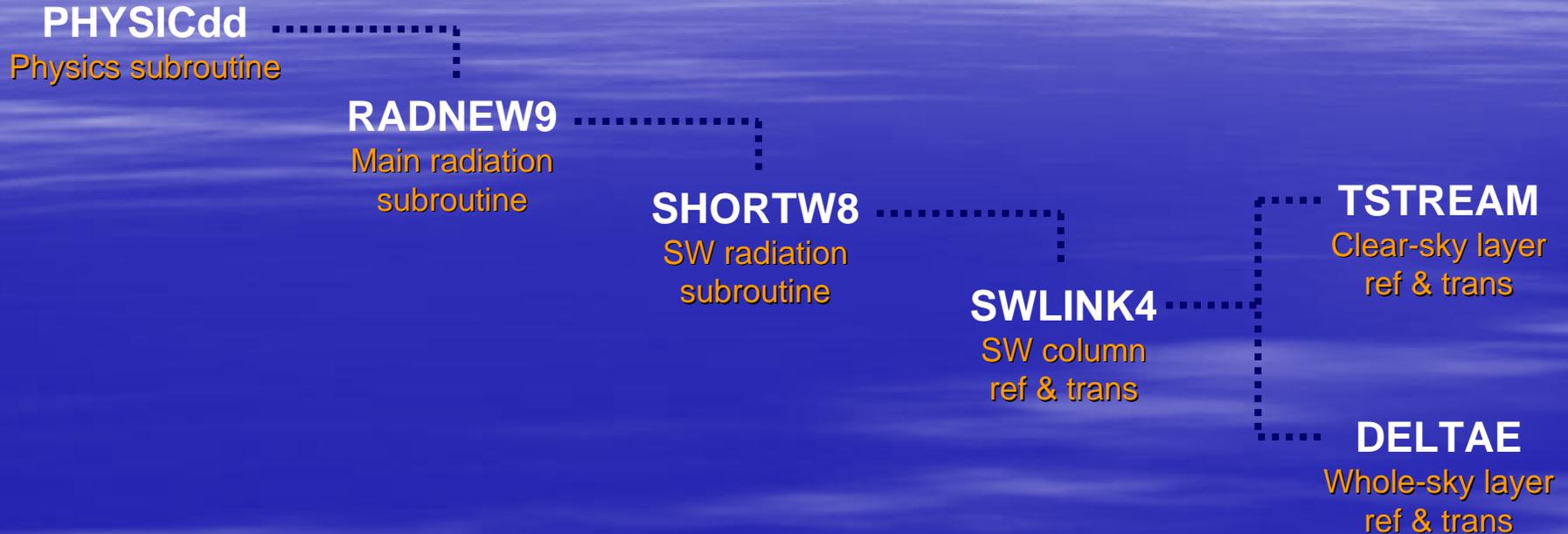
Jan



July



# Computational Time



Whole-sky computations: weighted by cloud fraction (CF)

$$\text{Layer Ref} = (1 - \text{CF}) \times \text{TS-Ref} + \text{CF} \times \text{DE-Ref}$$

$$\text{Layer Trans} = (1 - \text{CF}) \times \text{TS-Trans} + \text{CF} \times \text{DE-Trans}$$

# Computational Time

- Running-time ratio of modified to original SHORTW8: 2 – 3
- Arrays equivalenced in original scheme, so that TS computation is performed once
- Attempts to equivalence arrays for DFS code resulted in numerical errors, so clear-sky DFS has to be called again in whole-sky
- Potential to reduce running time of DFS-modified SW scheme

# Conclusions and Recommendations

- DFS code developed for SW radiation computations in CCC AGCM
- Significant changes in GCM computation of solar fluxes:
  - Whole-sky differences: within  $5 \text{ Wm}^{-2}$  TOA &  $10 \text{ Wm}^{-2}$  surface  
can be as large as  $+20$  and  $-40 \text{ Wm}^{-2}$
  - Clear-sky differences: within  $2 \text{ Wm}^{-2}$   
can be as large as  $+25$  and  $-12 \text{ Wm}^{-2}$
  - Percentage differences: 4–6% TOA &  $>20\%$  surface
- Most prominent at Tropics & high latitudes
- Mostly determined by cloud optical depth & solar zenith angle, and by aerosol optical depth in a clear sky

# Conclusions and Recommendations

- Chou (1992): accuracy of DFS computations in GCM within  $7.5 \text{ Wm}^{-2}$
- Reduction of computational time?
- Further research:
  - Improvement of the overall accuracy of GCM flux simulations  
(Closure experiments against observational data)
  - Implications to GCM simulation of climate dynamics